

## PRORACUN CILINDRICNOG ZUPCASTOG PARA

### Polazni podaci

- A1 Nominalna snaga  $P = 100\text{kW}$
- A2 Broj obrtaja pogon. masine  $n_1 = 1400\text{min}^{-1}$
- A3 Broj zubaca pogonskog zupčanika  $z_1 = 19$  usvojiti od 18 do 25
- A4 Broj zubaca gonjenog zupčanika  $z_2 = 30$  savet da  $z_1+z_2$  bude neparan broj
- A5 Prenosni odnos  $u = \frac{z_2}{z_1}$   $u = 1.579$
- A6 Ugao nagiba bocne linije  $\beta = 12\text{deg}$  usvojiti od 5 do 25 stepeni
- A7 Modul  $m_n = 6\text{mm}$  Tab. 4.2 str. 98
- A8 Ceoni modul  $m_t = \frac{m_n}{\cos(\beta)}$   $m_t = 6.134\text{ mm}$
- A9 Ugao nagiba profila  $\alpha_n = 20\text{deg}$
- A10 Faktor visine temenog dela alata  $h_{a0x} = 1.25$
- A11 Faktor polupreznika zaobljenja alata  $r_{oa0x} = 0.25$
- A12 Visina noge zupca  $h_{fp} = 1.25 \cdot m_n$   $h_{fp} = 7.5\text{ mm}$  od 10 do 40 % preko  $m_n$
- A13 Temeni zazor  $c = h_{fp} - m_n$   $c = 1.5\text{ mm}$
- A14 Sirina zupčanika  $b = 130\text{mm}$  usvojeno
- A15 Kvalitet izrade **IT 7** zadato
- A16 Materijal pogonskog zupčanika **C.1531 nitriran** Tab. 4.5 str. 133
- A17 Materijal gonjenog zupčanika **C.1331** usvojiti losiji materijal u odnosu na  $z_1$
- A18 Dinamicka izdržljivost bokova pog. zupčanika  $\sigma_{Hlim} = 950 \frac{\text{N}}{\text{mm}^2}$  Tab. 4.5 str. 133
- A19 Dinamicka izdržljivost podnozja pog. zupčanika  $\sigma_{Flim} = 300 \frac{\text{N}}{\text{mm}^2}$  Tab. 4.5 str. 133
- A20 Srednja hrapavost  $R_a = 1.6 \times 10^{-6}\text{ m}$  Tab. 1.1 str. 32 MEI

## Geometrija zupčanika

B1 Precnik podeone kruznice pog. zupčanika	$d_1 = m_t z_1$	$d_1 = 116.547 \text{ mm}$
B2 Precnik podeone kruznice gonj. zupčanika	$d_2 = m_t z_2$	$d_2 = 184.021 \text{ mm}$
B3 Ugao nagiba profila alata u ceonom preseku	$\alpha_t = \text{atan}\left(\frac{\tan(\alpha_n)}{\cos(\beta)}\right)$	$\alpha_t = 20.41 \text{ deg}$
B4 Nulto osno rastojanje	$a_r = \frac{(d_1 + d_2)}{2}$	$a_r = 150.284 \text{ mm}$
B5 Osno rastojanje	<b><math>a = 150 \text{ mm}</math></b>	(zaokruziti na blizu peticu)
B6 Precnik kinematske kruznice pog.zupčanika	$d_{w1} = 2 \cdot a \cdot \frac{z_1}{z_1 + z_2}$	$d_{w1} = 116.327 \text{ mm}$
B7 Precnik kinematske kruznice gonj.zupčanika	$d_{w2} = u \cdot d_{w1}$	$d_{w2} = 183.673 \text{ mm}$
B8 Ugao dodirnice	$\alpha_{wt} = \text{acos}\left[\frac{m_t(z_1 + z_2) \cdot \cos(\alpha_t)}{2 \cdot a}\right]$	$\alpha_{wt} = 20.117 \text{ deg}$
B9 Involut funkcija	$\text{inv}(x) = \tan(x) - x$	
B10 Zbir koef. pomeranja profila	$X = \left(\text{inv}(\alpha_{wt}) - \text{inv}(\alpha_t)\right) \cdot \frac{(z_1 + z_2)}{2 \cdot \tan(\alpha_n)}$	$X = -0.047$
B11 Parcijalni koef. pomeranja pogonskog zupčanika	<b><math>x_1 = 0</math></b>	
B12 Parcijalni koef. pomeranja gonjenog zupčanika	$x_2 = X - x_1$	$x_2 = -0.05$
B13 Precnik podnozne kruznice pog.zupčanika	$d_{f1} = d_1 + 2 \cdot x_1 \cdot m_n - 2 \cdot h_{fp}$	$d_{f1} = 101.547 \text{ mm}$
B14 Precnik podnozne kruznice gonj.zupčanika	$d_{f2} = d_2 + 2 \cdot x_2 \cdot m_n - 2 \cdot h_{fp}$	$d_{f2} = 168.457 \text{ mm}$
B15 Precnik temene kruznice pog.zupčanika	$d_{a1} = 2 \cdot a - d_{f2} - 2 \cdot c$	$d_{a1} = 128.543 \text{ mm}$
B16 Precnik temene kruznice gonj.zupčanika	$d_{a2} = 2 \cdot a - d_{f1} - 2 \cdot c$	$d_{a2} = 195.453 \text{ mm}$
B17 Precnik osnovne kruznice pog.zupčanika	$d_{b1} = d_1 \cdot \cos(\alpha_t)$	$d_{b1} = 109.23 \text{ mm}$
B18 Precnik osnovne kruznice gonj.zupčanika	$d_{b2} = d_2 \cdot \cos(\alpha_t)$	$d_{b2} = 172.468 \text{ mm}$
B19 Podeoni korak u normalnoj ravni	$p_n = \pi \cdot m_n$	$p_n = 18.85 \text{ mm}$
B20 Podeoni korak u ceonoj ravni	$p_t = \pi \cdot m_t$	$p_t = 19.271 \text{ mm}$
B21 Osnovni (sprezni) korak	$p_{et} = p_t \cdot \cos(\alpha_t)$	$p_{et} = 18.061 \text{ mm}$
B22 Aktivna duz.dodirnice	$g_\alpha = \frac{1}{2} \cdot \left(\sqrt{d_{a1}^2 - d_{b1}^2} + \sqrt{d_{a2}^2 - d_{b2}^2}\right) - a \cdot \sin(\alpha_{wt})$	$g_\alpha = 28.273 \text{ mm}$
B23 Stepen sprezanja profila	$\epsilon_\alpha = \frac{g_\alpha}{p_{et}}$	<b><math>\epsilon_\alpha = 1.565</math></b> mora biti $1 < \epsilon_\alpha < 2$
B24 Stepen sprezanja bocnih linija	$\epsilon_\beta = \frac{b \cdot \tan(\beta)}{p_t}$	<b><math>\epsilon_\beta = 1.434</math></b> iskustveno $1 < \epsilon_\beta < 1.5$
B25 Ukupni stepen sprezanja	$\epsilon_\gamma = \epsilon_\alpha + \epsilon_\beta$	$\epsilon_\gamma = 2.999$ najpogodnije u pogledu dinamike ako je ceo broj

B26 
$$\alpha_{tx1} = \operatorname{atan} \left[ \frac{1}{\cos(\alpha_t)} \cdot \sqrt{\sin(\alpha_t)^2 + 4 \cdot \frac{x_1}{z_1} \cdot \left(1 + \frac{x_1}{z_1}\right)} \right] \quad \alpha_{tx1} = 20.41 \text{ deg}$$

B27 
$$\alpha_{tx2} = \operatorname{atan} \left[ \frac{1}{\cos(\alpha_t)} \cdot \sqrt{\sin(\alpha_t)^2 + 4 \cdot \frac{x_2}{z_2} \cdot \left(1 + \frac{x_2}{z_2}\right)} \right] \quad \alpha_{tx2} = 19.92 \text{ deg}$$

B28 Ugao nagiba bocne linije 
$$\beta_b = \operatorname{asin}(\sin(\beta) \cdot \cos(\alpha_n)) \quad \beta_b = 11.267 \text{ deg}$$

B29 Merni broj zubaca z1 
$$z_{w1r} = \frac{z_1}{\pi} \cdot \left( \frac{\tan(\alpha_{tx1})}{\cos(\beta_b)^2} - \operatorname{inv}(\alpha_t) \right) - \frac{2 \cdot x_1 \cdot \tan(\alpha_t)}{\pi} + 0.5 \quad z_{w1r} = 2.744$$
  
na blizi ceo broj  $z_{w1} = 3$

B30 Merni broj zubaca z2 
$$z_{w2r} = \frac{z_2}{\pi} \cdot \left( \frac{\tan(\alpha_{tx2})}{\cos(\beta_b)^2} - \operatorname{inv}(\alpha_t) \right) - \frac{2 \cdot x_2 \cdot \tan(\alpha_t)}{\pi} + 0.5 \quad z_{w2r} = 3.958$$
  
na blizi ceo broj  $z_{w2} = 4$

B31 Mera preko zubaca pogonskog zupcanika

$$W_1 = m_n \cdot \cos(\alpha_n) \cdot \left[ \pi \cdot (z_{w1} - 0.5) + z_1 \cdot \operatorname{inv}(\alpha_t) \right] + 2 \cdot x_1 \cdot m_n \cdot \sin(\alpha_n) \quad W_1 = 45.983 \text{ mm}$$

B32 Mera preko zubaca gonjenog zupcanika

$$W_2 = m_n \cdot \cos(\alpha_n) \cdot \left[ \pi \cdot (z_{w2} - 0.5) + z_2 \cdot \operatorname{inv}(\alpha_t) \right] + 2 \cdot x_2 \cdot m_n \cdot \sin(\alpha_n) \quad W_2 = 64.487 \text{ mm}$$

## Opterećenje

C1 Faktor spoljasnih dinamičkih sila  $K_A = 1.25$  Tab.4.3 str.127 za ravnomeran rad

C2 Ugaona brzina pogonskog zupcanika  $\omega_1 = 2 \cdot \pi \cdot n_1 \quad \omega_1 = 146.608 \text{ s}^{-1}$

C3 Obrtni moment na pogonskom vratilu  $T_1 = \frac{P}{\omega_1} \quad T_1 = 682.093 \text{ N}\cdot\text{m}$

C4 Obimna sila na podeonom cilindru pog.zupcanika  $F_{t1} = \frac{2 \cdot T_1}{d_1} \quad F_{t1} = 1.171 \times 10^4 \text{ N}$

C5 Obimna sila na podeonom cilindru gonj.zupcanika  $F_{t2} = F_{t1} \quad F_{t2} = 1.171 \times 10^4 \text{ N}$

C6 Obimna brzina zupcanika  $v = \frac{d_1}{2} \cdot \omega_1 \quad v = 8.543 \frac{\text{m}}{\text{s}}$

C7 Parametar brzine  $\frac{v \cdot z_1}{100} = 1.623 \frac{\text{m}}{\text{s}}$

C8 Faktor unutrašnjih dinamičkih sila  $K_{V\beta} = 1.07$  Sl. 4.47 str. 128

$$K_{V\alpha} = 1.13$$

za  $\varepsilon_\beta = 1.434 \quad \varepsilon_\beta > 1 \quad K_V = K_{V\beta} \quad K_V = 1.07$

C9 Faktor raspodele opterećenja  $K_{H\beta} = 1.08$  Tab. 4.4 str. 130 za  $\frac{b}{d_1} = 1.115$

C10 Ukupni faktor opterećenja  $K_H = K_A \cdot K_{V\beta} \cdot K_{H\beta} \quad K_H = 1.445$

**Nosivost u odnosu na cvrstocu bokova zubaca**

D1 Faktor elasticnosti materijala  $Z_{Ec} = 189 \sqrt{\frac{N}{\text{mm}^2}}$  za kontakt celik po celiku

$Z_{Esl} = 163 \sqrt{\frac{N}{\text{mm}^2}}$  za kontakt celik po sivi liv

D2 Uticaj elasticnosti materijala  $Z = 2.5 \cdot Z_{Ec} \cdot \cos(\beta)$   $Z = 462.175 \sqrt{\frac{N}{\text{mm}^2}}$

D3 Radni napon boka zupca  $\sigma_H = Z \cdot \sqrt{\frac{F_{t1}}{b \cdot d_1} \cdot \frac{u+1}{u} \cdot K_H}$   $\sigma_H = 623.975 \frac{N}{\text{mm}^2}$

D4 Kriticni napon bokova  $\sigma_{Hkr} = \sigma_{Hlim}$   $\sigma_{Hkr} = 950 \frac{N}{\text{mm}^2}$

D5 Stepen sigurnosti obzirom na bok zupca  $S_H = \frac{\sigma_{Hkr}}{\sigma_H}$   $S_H = 1.5$  **zadovoljava**

D6 Dozvoljeni stepen sigurnosti protiv razaranja bokova zubaca  $S_{Hd} = 1.2$

$S_{Hd} = 1.2$  do 2 po preporuci

**Nosivost u odnosu na cvrstocu podnozja zubaca**

E1 Faktor koncentracije napona  $Y_{\Pi} = 1.92$  za  $m_n = 6 \text{ mm}$

$Y_{\Pi} = 2$  za  $m_n \leq 5$  i  $R_a \leq 10 \cdot \mu\text{m}$  manje vrednosti uzimati za vece  $R_a$   
 $Y_{\Pi} = 1.7 + 2$  za  $m_n > 5$  i/ili  $R_a > 10 \cdot \mu\text{m}$

E2 Kriticni napon  $\sigma_{FM} = Y_{\Pi} \cdot \sigma_{Flim}$   $\sigma_{FM} = 576 \frac{N}{\text{mm}^2}$

E3 Faktor oblika zupca  $Y_{Fa} = 2.91$  Tab.4.8 str.139

$z_n = \frac{z_1}{\cos(\beta)^3}$   $z_n = 20.3$  i  $x_1 = 0$  iz geometrije

E4 Faktor koncentracije napona  $Y_{Sa} = 1.66$  Sl.4.54 str.137

E5 Faktor polozaia  $Y_{\epsilon} = 0.25 + \frac{0.75}{\epsilon_{\alpha}}$   $Y_{\epsilon} = 0.729$

E6 Uticaj oblika kosozubih zupcanika  $Y_{\beta} = 1 - \epsilon_{\beta} \cdot \frac{\beta}{120\text{deg}}$   $Y_{\beta} = 0.857$

E7 Faktor raspodele opterecenja  $K_{F\beta} = 1.06$  Tab.4.4 str.130 za  $K_{H\beta} = 1.08$

E8 Napon u podnozju zupca  $\sigma_F = Y_{Fa} \cdot Y_{Sa} \cdot Y_{\epsilon} \cdot Y_{\beta} \cdot \frac{F_{t1}}{b \cdot m_n} \cdot K_A \cdot K_V \cdot K_{F\beta}$   $\sigma_F = 64.188 \frac{N}{\text{mm}^2}$

E9 Stepen sigurnosti obzirom na lom zupca  $S_F = \frac{\sigma_{FM}}{\sigma_F}$   $S_F = 9$  **zadovoljava**

$S_{Fd} = 1.4$  preporuka za dozvoljeni stepen sigurnosti